



Developing Software Rigorously: Introduction and Motivation¹

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¹Many slides borrowed from J. R. Abrial and M. Butler (日) (個) (目) (日) (日) (の) ◆□ > ◆母 > ◆臣 > ◆臣 > 善臣 の Q @ Take notes Plan w l 🖉 nez To Remember a Lecture Better, Take Notes by Hand Students do worse on guizzes when they use keyboards in class • Three-hour lectures: three 50-minute sections with ten-minute breaks. • Worked well in previous years. • Course: two parts. • Homework + term project with presentation. • Final exam for those who **choose not** to do HW + project. • Hands-on. Picture & headline ©*The Atlantic* https://www.theatlantic.com/technology/archive/2014/05/to-remember-a-lecture-better-take-notes-by-hand/361478/

I will make notes / slides available *after* the lectures I will ask you to work during the lectures

Purpose of the course





- To give you some insights about modelling and formal reasoning
- To show that programs can be *correct by construction*
- To show that modelling can be made practical
- To illustrate this approach with many examples

By the end of the course you should be comfortable with:

- Modelling (versus programming)
- Abstraction and refinement
- Some mathematical techniques used to reason about programs
- The practice of proving as a means to construct (provably) correct programs
- The usage of some tools to help in the above

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Software is omnipresent in everyday life

Large interconnected systems: independent, isolated, automatic decision making (which must be globally correct).



Software is omnipresent in everyday life

- Cell phones (from O.S. to compression algorithms to user interfaces).
- HDTV (routing, encoding and decoding), Netflix, ...
- Buying and selling on the Internet (web interfaces, databases, encryption).
- Stock market (algorithmic trading, high frequency trading).
- Skype, Whatsapp, AirBnB, idealista, GroupOn, FB, Steam, Spotify, E-Banking, Google Maps / Waze, Uber / Lyft, ...





- \checkmark Managed by extremely complex and intelligent software.
- \sqrt{AII} of them *critical* to a certain degree.
- √ Some **extremely** critical



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Overall challenge:

How to develop complex software, with resources that are **always limited**, ensuring that it will work correctly?

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Growth in complexity and expectations



Then and now



	Yesterday	Today	Tomorrow
	It's nice that I can		
 Processes managed by computing systems increasingly complex. 	see my account		
 Same software is to run in several platforms. 	through my web browser!		
 Computing systems interact more and more with other systems. 			

- They should stay autonomous for longer.
- They become reactive.



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Then and now



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Then and now







Then and now



How far are we from giving reasonable guarantees? (Only showing some types of problems)



Skype bug sends messages to unintended recipients.



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- Still infected, 300,000 PCs to lose Internet access.

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iOS, Mac app crashes linked to botched FairPlay DRM.

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- July 16, 2012: Skype bug sends messages to unintended recipients.
- July 13, 2012: Apple's "in-app purchase" service for iOS bypassed by Russian hacker.
- July 13, 2012: German security experts find major flaw in credit card terminals.
- July 13, 2012: Defects leave critical military, industrial infrastructure open to hacks (Niagara Framework, linking 11+ million devices in 52 countries).
- July 12, 2012: Hackers expose 453,000 credentials allegedly taken from Yahoo service.
- July 12, 2012: Mountain Lion (Mac OS X version) sends some 64-bit Macs to sleep (related to graphics drivers).
- July 7, 2012: Still infected, 300,000 PCs to lose Internet access.
- July 6, 2012: Apple fixes App Store DRM error, crash-free downloads resume.
- July 5, 2012: "Find and Call" app becomes first trojan to appear on iOS App Store.
- July 5, 2012: iOS, Mac app crashes linked to botched FairPlay DRM.

Just two weeks

The Ariane 5 incident

Example: effect of a *single* overflow





The Ariane 5 incident

Example: effect of a single overflow



- June 4, 1996: After launch, the Ariane 5 rocket exploded.
- This was its maiden voyage.
- It flew for about 37 Sec only in Kourou's sky.
- No injury in the disaster.

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The story



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More details



- Normal behavior of the launcher for 36 Sec after lift-off
- Failure of both Inertial Reference Systems almost simultaneously
- Strong pivoting of the nozzles of the boosters and Vulcan engine
- Self-destruction at an altitude of 4000 m (1000 m from the pad)

- Both inertial computers failed because of overflow on one variable
- This caused a software exception that stopped these computers
- These computers sent post-mortem info through the bus
- Normally, main computer receives velocity info through the bus
- The main computer was confused and pivoted the nozzles

More details

How?



Messages



- The faulty program was working correctly on Ariane 4
- The faulty program was not tested for A5 (since it worked for A4)
- But the velocity of Ariane 5 was far greater than that of Ariane 4
- That caused the overflow in one variable
- The faulty program happened to be useless for Ariane 5

- Clear, up to date, realistic requirements
- Relationship requirements / programs
- Proof that programs were built according to requirements

Note: we will not deal with requirement engineering, *which is related and very interesting in itself.*

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software		How?	5	software
• How can we ensure that a program does what it is supposed to do?		 How can we ensure that a program does what it is supposed to do?)	
			 How do we state what is it supposed to do? (usually via specifications) 	

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software

- How can we **ensure** that a program does what it is supposed to do?
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How?

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- How can we **ensure** that a program does what it is supposed to do?
 - 1. How do we state what is it supposed to do? (usually via *specifications*)
 - 2. How do we build the program?
 - 3. How do we prove that the program performs according to specifications?
 - ... in a way that is (a) dependable and (b) cost-effective?

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Cost of error fixes

Rate of error discovery



🔤 i 🕅 dea (🗵) The V model The V model i dea software software When are errors discovered in the V Model? When are errors discovered in the V Model? Validation testing Validation testing Specification Specification Preliminary design Integration testing Many specification errors are detected only after a lot of development has been undertaken Unit testing Detailed design

Coding

Coding

Some sources of errors

- Lack of precision
 - Ambiguities
 - Inconsistencies
- Too much complexity
 - Complexity of requirements
 - Complexity of operating environment
 - Complexity of designs

Some sources of errors

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Some preventive measures

- Early stage analysis
 - Precise descriptions of intent
 - Amenable to analysis by tools
 - Identify and fix ambiguities and inconsistencies as early as possible
- Mastering complexity
 - Encourage abstraction
 - Focus on what a system does
 - Early focus on key / critical features
 - Incremental analysis and design

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Formal methods

- software
- Rigorous techniques for formulation and analysis of systems
- They facilitate:
 - Clear specifications (contract)
 - Rigorous validation and verification

If we do not capture precisely what a system ought to do, there is little chance that we may really decide whether it fits the bill

Validation: does the contract specify the right system?

• Answered informally

Verification: does the finished product satisfy the contract?

• Can be answered formally

Specifications and the real world?



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How can specifications be used?

- Use a specification to build tests
- Use a specification to check that a program computes what it should (verification, model checking)
- Use a specification to compute (functional / logic / equational programming)
- Use specifications to drive the generation of a program (correctness by construction, automatic code generation)



How can guarantees be given?



How can guarantees be given?

- Enlightened management: of little help.
- Convincing arguments beyond any reasonable doubt:
 - Formal basis.
 - Proofs based on rigorous methods.
- Carefully prove that programs will behave as expected.

- Enlightened management: of little help.
- Convincing arguments beyond any reasonable doubt:
 - Formal basis.
 - Proofs based on rigorous methods.
- Carefully prove that programs will behave as expected.
- For **every** single program?



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It's too difficult for humans to do!





MethodologiesMechanization

development

• Computer-aided software

• Automatic analysis

Automated testing

• Correctness by construction

• Verification (model checking,

deductive verification)

Automation

A basic property: termination

- Termination is often expected.
- How easy is it to decide whether a program terminates?

input n;

```
while n > 1 do
    if n mod 2 = 0 then
        n:= n / 2
    else
        n:= 3*n + 1
    end if
end while
```

Question: will it finish for any input value n?

A specification example



• What does this program do?



A specification example



procedure whatAmI(A: Array) repeat swapped := false for i := 1 to length(A) - 1 do if A[i-1] > A[i] then swap(A[i-1], A[i]) swapped := true end if

end for until not swapped end procedure

• What does this program do?

• Can you specify (using FOL) the property that characterizes a sorted array?

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A specification example

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```

- What does this program do?
- Can you specify (using FOL) the property that characterizes a sorted array?
- Can we prove that, after executing the code above, array A meets that property?
- Can we use specifications to derive a correct sorting program?



Jean-Raymond Abrial. Faultless systems: Yes we can! *IEEE Computer*, 42(9):30–36, 2009.

Jean-Raymond Abrial. *Modeling in Event-B - System and Software Engineering.* Cambridge University Press, 2010.